

Energy-efficient GPS synchronization for wireless nodes

David Pallier, Vincent Le Cam, Sébastien Pillement

Abstract—Synchronization is a challenging problem for wireless nodes, especially for applications demanding good synchronization accuracy over wide areas. In that case, the GPS is a valuable solution as the nodes can independently synchronize to UTC. However, the energy consumption of a GPS receiver (over 100 mW when switched on) is not sustainable on a wireless node. Therefore, in this work, we developed a synchronization scheme based on periodic extinctions of the GPS receiver. The goal is to study the GPS power switching effect on the synchronization accuracy. To do so, a node with dedicated timestamping hardware was designed. Two clock models were compared to predict the node time when the GPS is off and the impact of a Kalman filter, to remove the GPS noise, was evaluated. From experimental data, we show that the choice of the clock model depends on the accuracy needed and that the Kalman filter improves the estimation of the clock frequency for both models. In our design, the GPS can be off from 60% up to 95% of the time for mean synchronization errors of 20 ns to 420 ns, respectively. This work demonstrates that GPS power switching is an efficient solution to reduce energy costs while maintaining a high synchronization accuracy.

Index Terms—Clock synchronization, WSN, Energy efficiency, FPGA, GPS, Kalman filter, Structural Health Monitoring

I. INTRODUCTION

MONITORING the health of structures often implies the deployment of many sensor nodes to sample physical parameters such as ambient temperature, constraints, vibrations, acoustic waves, electrical fields, etc. Posted to a central supervisor, in delayed or in real-time, those samples are fed to Structural Health Monitoring (SHM) algorithms to assess the infrastructure health. As most of these parameters are time-dependent and sampled from different nodes, the system needs to have a common time reference. The following examples underline the need for synchronization and the accuracy needed for SHM applications:

- 1) The natural frequency range of vibrations for structural diagnostics (modal analysis) is typically comprised between 0 and 100 Hz. Thus, accelerations are usually sampled at 1000 Hz. To ensure good modal reconstruction, the synchronization error between nodes must be lower than 1 ms.
- 2) Acoustic wave propagation is often used to localize the crack origin in a steel bar or a wire break in bridge cables. The method based on Time Difference Of Arrival (TDOA) is very dependent on the sensor's ability to timestamp acoustic wavefronts. With a typical velocity of 5000 m/s and a localization accuracy expected to ± 15 cm, synchronization error between two nodes must be lower than 30 microseconds.
- 3) The TDOA method is also used to monitor the localization of lightning on high electrical voltage lines. With

a speed of 200 000 km/s and an expected localization of ± 50 m, synchronization error between two nodes must be under 250 nanoseconds.

Time-counting on an electronic device, such as a wireless node, is mainly based on the use of an oscillator. Unfortunately, oscillators are highly sensitive to environmental conditions such as temperature, acceleration, or voltage supply stability [1]. Consequently, the frequency of the oscillator drifts from its theoretical value over time. Without a synchronization protocol, each node will have its own local time and the offset between the clocks of the nodes increases over time. In most of the cases, this synchronization protocol relies on timestamps exchange between the nodes. The synchronization accuracy that can be obtained in the network depends on the accuracy of the timestamps exchange, the synchronization update rate, and the stability of local oscillators.

A wireless sensor network (WSN) is a cost-effective way to deploy sensing nodes onto already existing large structures (bridges, wind power plants, railway lines, etc). This is why WSNs are more and more used for SHM applications. However, synchronization between nodes is harder in wireless networks due to non-deterministic propagation delays. Classical wireless synchronization protocols such as [2], [3] and [4] cannot achieve sub-microsecond accuracy, especially in multi-hop scenarios. In this context the Precision Time Protocol (PTP) has been extended over 802.11 communications with hardware timestamping [5] or synchronization over UWB communications [6] and can achieve sub nanosecond accuracy. While these protocols can offer good synchronization accuracy for the monitoring of small structures, they cannot be used for large structures like bridges, railways or power-lines, as they need close and iterative synchronization process. For large outdoor systems (which are most of SHM applications) a satel-

This work was supported by the WISE program of Pays-de-la-Loire region

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1
2 lite navigation system, like GPS, can be used to synchronize
3 each node to UTC as in [7]. This method is suitable for large
4 infrastructures and allows timestamping accuracy up to tens
5 of nanoseconds. The main limitation of this technique is the
6 energy cost of a GPS receiver. Since energy consumption
7 needs to be minimized in wireless systems, GPS solution
8 needs to be optimized according to the required timestamping
9 accuracy.

10 In this context, we developed a new synchronization scheme
11 based on GPS holdover. Namely, GPS is used for precision
12 purpose but it will be turned off to save power. During the
13 off-state, the local time of the node is estimated using a
14 clock model. The synchronization accuracy obtained with this
15 scheme depends on the chosen holdover parameters: from
16 tens of ns to 1 ms. To further improve the estimation of
17 the clock model parameters, the GPS signal can be filtered
18 when in on-state. The contributions of this work are: (1) the
19 design of a node with dedicated hardware for timestamping,
20 (2) the accuracy and energy efficiency evaluations of our
21 synchronization scheme for different clock models, and (3)
22 the study of the impact of frequency filtering using a Kalman
23 filter.

24 The paper is organized as follows. The related works
25 are summarized in Section II. Node architecture, timestamps
26 computation, the use of GPS for periodic re-synchronization
27 and the experimental setup are described in Section III. Section
28 IV introduces the clock models, and the Kalman filter. The
29 results are discussed in Section V, while Section VI resumes
30 our contributions and outlines future perspectives.

31
32 **II. RELATED WORKS**

33
34 Since synchronization in distributed systems was first for-
35 malized in [8] and later extended in [9], numerous solutions
36 have been developed to tackle the problem of synchroniza-
37 tion in networks. The Network Time Protocol [10] and the
38 Precision Time Protocol [11] are the most used network syn-
39 chronization protocols over the wired Ethernet. It is possible
40 to obtain microsecond synchronization accuracy with these
41 protocols, and an extension of the PTP [12] aims to achieve
42 sub-nanosecond accuracy.

43 Classical synchronization protocols for WSNs are based on
44 the exchange of dedicated timestamped RF beacons. These
45 protocols can be divided into two categories: the sender to
46 receiver and the receiver to receiver protocols. In the sender
47 to receiver scheme, a node sends its time to a receiver that
48 timestamp the arrival of the packet using its local time.
49 Then, the receiver synchronizes itself by estimating the offset
50 between its local time and the time of the sender. To estimate
51 the propagation delay a two-way exchange has been developed
52 in [3]. The same principle is used in [4] but on a mesh
53 topology instead of a tree and with the estimation of the packet
54 processing overhead. Other works [13] [14] [15] also rely on
55 the same principle but are optimized for specific nodes with
56 constrained resources like PicoRadios [16]. In the receiver
57 to receiver scheme [2] [17] a third party node broadcast a
58 beacon that doesn't contain a timestamp. All the receivers
59 timestamp the arrival of the beacon with their local clock

and then exchange their observations pairwise to calculate
their offsets. The performances of all these protocols are
limited by the propagation delays and the packet processing
overhead. The interested reader can refer to [18] that outlines
the existing implementations of these techniques and their
limitations. While some implementations of these protocols
can achieve microsecond accuracy most of them are in the
tens of microsecond range. Moreover, the accuracy decreases
with the number of hops which can be problematic on large
structures such as bridges, railways, or power-lines. Signal
processing techniques have been described in [19] to deal with
non-deterministic propagation delays but, to the best of our
knowledge, these techniques have not been implemented on
real wireless nodes.

Other works focus on the implementation of clock syn-
chronization in wireless communication norms. ZigBee is the
most used protocol in the Low Rate Wireless Area Personal
Network (LR WPAN), which adds network and application
layers on top of the 802.15.4 protocol. In [20] the Flooding
Time Synchronization Protocol (FTSP) is used to synchronize
nodes over ZigBee to obtain a timestamping accuracy of 61
 μ s. The use of UWB for the physical layer was added to
IEEE 802.15.4 as an amendment in 2007 and merged in
IEEE 802.15.4-2011. In [6] UWB is used to synchronize
the clocks of a pair of chips on the same PCB with an
accuracy of 374 ps (standard error of 677 ps). Several im-
plementations of synchronization protocols over IEEE 802.11
are compared in [21]. IEEE 802.11 compliant synchronization
solutions can achieve μ s clock synchronization accuracy [22]
and non compliant solutions using PTP (IEEE 1588) can
achieve nanosecond accuracy [5] or sub-nanosecond accu-
racy with a hardware timestamping mechanism. While these
synchronization schemes can offer a good synchronization
accuracy on small structures, they are not suited for large
structures, where the nodes can be distant of a few hundred
meters to several kilometers. More recently, Low-Power Wide-
Area Network (LPWAN) communications have gained interest
for industrial applications. Based on LoRa, Sigfox, or NB-
IoT, these protocols allow for communications over a few
kilometers in urban areas. In [23] LoRa and NB-IoT are used
for node communications in the context of machine vibrations
monitoring. Nodes are synchronized every 10 s using LoRa
with an accuracy of 5 μ s.

Another approach to wireless node synchronization is to
use a satellite navigation system, like the GPS, to make
each node synchronized to UTC. This solution has been
implemented in [7] and [24]. The clock of the node is steered
by the PPS signal coming out of its GPS receiver. To achieve
an accuracy of tens of nanosecond, dedicated hardware is
used with high-speed counters. The use of hardware induces
deterministic timestamping which removes software overhead
and thus improves the timing accuracy. While this approach is
suitable for accurate synchronization, a GPS receiver requires
a lot of energy (up to 100 mW). This cost can be affordable
for applications requiring a high synchronization accuracy,
but for less critical applications that require less accuracy,
the energy consumption needs to be optimized. In this work,
we propose an adaptive synchronization protocol based on

automatic on/off switching of the GPS receiver to minimize the energy consumption under a defined accuracy constraint.

Adaptable synchronization accuracy has already been described in [17] as an extension of RBS [2]. In [25] a Kalman filter is used to track the offset of a local clock from timestamped message exchange and an algorithm is developed to find the optimal message exchange rate for a parametric accuracy. Our work differs from these solutions as it is designed on top of GPS synchronization (although any GNSS receiver can be used) instead of beacons exchange and relies on dedicated timestamping hardware to achieve up to tens of nanoseconds synchronization accuracy.

III. WIRELESS NODE

A. Node Architecture

The node design presented in this paper is similar to the one presented in [7]. It includes a dedicated hardware timestamping unit. The timestamping unit is connected to a GPS receiver and has inputs connected to digital signals that have to be timestamped (see Figure 1). The node is synchronized with the PPS signal and the epoch transmitted on a serial link from the GPS receiver. A rising edge on the PPS signal corresponds to the beginning of a UTC second. The epoch corresponds to the number of seconds elapsed since January 6th, 1980. It is used to compute the UTC date at the next rising edge of the PPS signal. The detection of a rising or a falling edge on a digital input of the node is called an event. The events are timestamped with high-speed counters in the timestamping unit and are stored until they are read by the main control unit of the node. This node architecture has several advantages:

- *No processing overhead:* The use of dedicated hardware on FPGA suppress processing overhead at event detection. Since the delay between the rising edge on the input and the timestamping is deterministic and not affected by software overhead due to process scheduling and interrupt latency, the timestamping accuracy is improved.
- *Parallel high granularity timestamping:* On most microcontroller units, the number of parallel counters able to timestamp independent events is limited. Another limiting factor is the time granularity fixed by the quartz oscillator frequency. With a custom design, the number of parallel counters is only limited by the FPGA size. The frequency is fixed by the PLL included in the FPGA and can be higher than the quartz oscillator frequency, allowing a higher granularity.
- *Asynchronous data fetching and main control unit independence:* Since timestamping and data processing are separated, the main control unit can fetch data (on digital inputs) asynchronously on the timestamping unit. Thus any operating system and any microcontroller can be used as long as the microcontroller is equipped with a serial link.

In this work, we focus on the timestamp unit design. For the main control of the node, without loss of generality and for quick prototyping purposes, we used a Raspberry Pi.

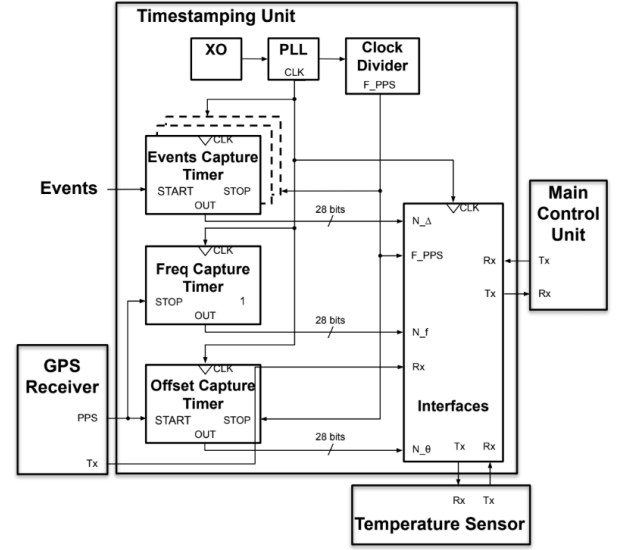


Fig. 1: Timestamp unit

B. Timestamp computation

We define the local estimation of the PPS signal (according to the local quartz oscillator) as the fake PPS signal. The offset θ is then the time between a rising edge of the true PPS signal and the next rising edge of the fake PPS signal (issued by the GPS). It corresponds to the time difference between the local clock and the GPS time. Δ is the time between a rising edge of the fake PPS signal and a rising edge on a digital input (i.e. an event). θ and Δ are represented in the timing diagram in Figure 2.

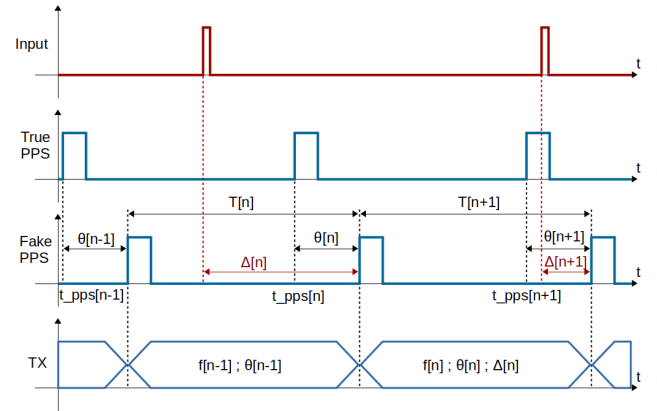


Fig. 2: Timing diagram

The date $t[n]$ of a recorded event occurring during the n^{th} local second is computed based on the date of the true PPS rising edge $t_{pps}[n]$, that occurred during the fake PPS period and the elapsed time between the event and this rising edge. The elapsed time corresponds to the measured offset $\theta[n]$ minus the measured $\Delta[n]$ for this particular event. This time is positive when the event is detected after the true PPS edge and negative when detected before. Hence:

$$t[n] = t_{pps}[n] + \theta[n] - \Delta[n] \quad (1)$$

C. Timestamping unit Architecture

The above timestamp computation is implemented on a Spartan 6 FPGA and is shown in Fig. 1. Since this design aims at turning off the GPS, the clock synchronization is different from the one used in [7]. In this design, the clock counter is not reset by the PPS but instead is bounded by N_0 . This integer corresponds to the number of clock beats counted over one second at the nominal frequency f_0 of the quartz oscillator. In the meantime, the local time offset θ is recorded to convert the local timestamp to UTC. The fake PPS signal is generated inside the FPGA, by dividing the local clock frequency to obtain a 1Hz square signal. The offset corresponds to the differential between this signal and the true PPS signal from the GPS receiver. Tracking the local time offset has been chosen over the control of the clock as it allows for both offline and online synchronization. This enables us to perform the timestamp conversion, from local time to UTC, on the fly or post facto if the offset is recorded alongside the events. This post facto synchronization allows us to test different synchronization schemes from the same events dataset for evaluation purposes.

The values θ and Δ are not directly measured inside the timestamp unit as they are integers corresponding to counter values and not timing values. Let N_θ and N_Δ be the counter values corresponding to the offset counter and the event counter, respectively. These integers are converted into time values using the true frequency of the oscillator. Equation 1 becomes:

$$t[n] = t_{pps}[n] + \frac{1}{f[n]}(N_\theta[n] - N_\Delta[n]) \quad (2)$$

With N_f , N_θ and N_Δ the counter values from the timestamp unit, while t_{pps} is obtained from the GPS receiver.

The number of local clock beats counted during a full period of the true PPS signal is N_f . Let T_{GPS} be the time elapsed between two rising edges of the true PPS signal. If the true PPS signal is perfect then T_{GPS} is one second. The true frequency of the local oscillator can be computed as follows:

$$f[n] = \frac{N_f[n]}{T_{GPS}[n]} \quad (3)$$

giving:

$$t[n] = t_{pps}[n] + \frac{T_{GPS}}{N_f[n]}(N_\theta[n] - N_\Delta[n]) \quad (4)$$

If the true PPS signal is perfect, the only residual error is due to the granularity resolution as N_f , N_θ and N_Δ are integer values. The frequency output of the PLL inside the FPGA was set to 240MHz giving a counter resolution of 4.17 ns.

D. Periodic re-synchronization from GPS

As described in [26], GPS synchronization allows for a timing accuracy under 60ns. However, it entails a substantial energy cost as the GPS receiver is constantly on. When a lower accuracy is needed, GPS can be used periodically to re-synchronize the node. Between two synchronizations, the GPS receiver is off to save energy. The accuracy that can be obtained depends on the re-synchronization period. To be able

to deliver the PPS and the epoch, the GPS receiver needs to decode parts of the navigation message broadcasted by the GPS satellites. In normal conditions the GPS receiver has to:

- Generate PPS: In order to generate the PPS signal, the GPS receiver needs to track the "in-view" satellites, compute its time and position (called fix) and then lock its clock. According to [26] the time to first fix is under 1 second when the ephemeris are still valid. From experimentations, we observed less than 1 second to get a fix and less than 4 seconds to lock the clock.
- Refresh ephemeris: In order to track the in-view satellites the receiver needs to compute its position, therefore the ephemeris needs to be updated. In this work, we update them at their typical update rate of two hours.
- Acquire a complete navigation message: Since the ephemeris are already acquired every two hours the complete navigation message is acquired once a day.

In between the above phases, we propose to turn on and off the GPS to save energy. The off phase is called holdover and correspond to the time between two consecutive GPS time synchronizations. Figure 3 shows the on and off phases of the GPS receiver for a 24 hours period. The T_{NAV} is 25 minutes long every 24 hours. The T_{EPH} is 1 minute long every 2 hours. The GPS is on during k_{on} seconds and in holdover during $k - k_{on}$ seconds. In this mode, the GPS receiver is switched off (except its memory to keep the ephemeris). Equation 5 gives r , which represents the on/off ratio of the GPS receiver over 24 hours as a function of the parameters k , k_{on} , T_{NAV} and T_{EHP} .

$$r = T_{NAV} + \frac{1}{86400} \cdot (k_{on} \cdot \frac{7200 - T_{NAV}}{k} + 11 \cdot k_{on} \cdot \frac{7200 - T_{EHP}}{k}) \quad (5)$$

The minimum k_{on} is 5 seconds to get at least one locked pulse on the PPS signal, after this first delay the receiver delivers one pulse per second. Two pulses are required to get N_θ , N_Δ and N_f . The main difficulty is then to track the offset of the fake PPS, while the GPS is in holdover mode.

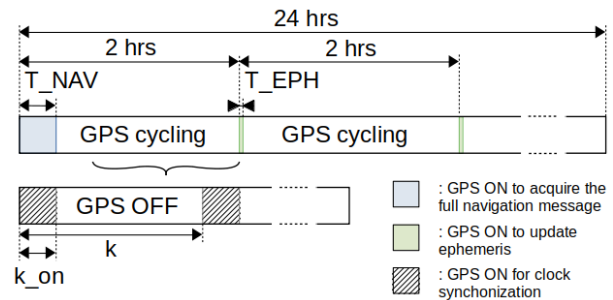


Fig. 3: Synchronization process from GPS

IV. OFFSET TRACKING

A. Clock model

The offset needs to be predicted during the holdover to have accurate timestamping. To do so a clock model is used. Let

$C(t)$ be the node local time as a function of the real time.

$$C(t) = \int_0^t \omega(\tau) d\tau + \theta_0 \quad (6)$$

With ω the clock rate and θ_0 the offset at the origin. A perfect clock would yield $C(t) = t$. The $C(t) = \omega \cdot t + \theta$ model is often used [2] [4]. In this model, the clock rate is constant but not equal to one. This is due to the fact that most of the oscillators are not functioning at their nominal frequency, but at a frequency supposed to be constant. While the latter is known to be false for crystal quartz oscillator, the variations of the frequency over a short time can be small enough to be considered constant since ambient temperature moves slowly. Fig. 4 represents the local time as a function of the real time for a perfect clock, a clock with a constant rate and a clock with a varying rate. The oscillator used in this design is an SPXO with an overall frequency stability of ± 20 ppm. Typically, the frequency stability of these oscillators is in the ppb range for sampling intervals of one second [21].

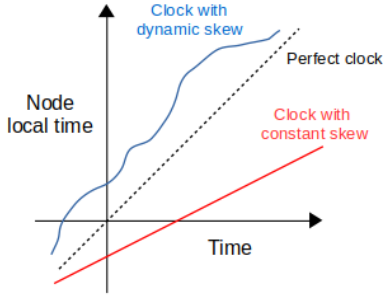


Fig. 4: Constant and dynamic skew of the local time over UTC

The offset of a clock at time t is the difference between its local time $C(t)$ and the real time t . Thus the local time offset $\theta(t)$ can be expressed as:

$$\theta(t) = C(t) - t \quad (7)$$

$$= \int_0^t \omega(\tau) d\tau + \theta_0 - t \quad (8)$$

Since the offset is sampled every second in the node, a discrete time model is needed. Equation 8 becomes:

$$\theta[n] = \sum_{i=1}^n \omega[i] \cdot \tau[i] - \sum_{i=1}^n \tau[i] + \theta_0 \quad (9)$$

With τ representing the duration of a supposed second for the node. This duration depends on the frequency of the node's oscillator and can be expressed as:

$$\tau[n] = \frac{N_0}{f[n]} = \frac{N_0}{N_f[n]} \cdot T_{GPS}[n] \quad (10)$$

The clock rate $\omega[n]$ can be computed from the number of local clock beats counted during $T_{GPS}[n]$:

$$\omega[n] = \frac{N_f[n]}{N_0} \quad (11)$$

Therefore:

$$\theta[n] = \sum_{i=1}^n T_{GPS}[i] - \sum_{i=1}^n \tau[i] + \theta_0 \quad (12)$$

If the PPS is considered perfectly synchronized to UTC, $T_{GPS} = 1s$ and thus:

$$\theta[n] = n - \sum_{i=1}^n \frac{N_0}{N_f[i]} + \theta_0 \quad (13)$$

In holdover mode, τ is not known since the GPS receiver is off. The simplest method to estimate it is to use its last value that was observed when the GPS was on. Since the error on the offset is the sum of the error on τ , this error will grow as τ drift away from its last observed value. In that case, the synchronization accuracy will depend on the holdover time and the drift rate of τ . This model will now be referred to as the Constant Skew Clock Model (CSCM).

Another model, that will be referred to as the Linear Skew Clock Model (LSCM), is to consider that τ is evolving linearly during the holdover mainly due to slow variations of the ambient temperature. In this model, the clock skew is considered as dynamic (see Fig. 4) and approximated by a piecewise linear function. The clock skew can be computed as:

$$\tau[n+1] = \tau[n] + u \quad (14)$$

with u the common difference that can be evaluated for every holdover as:

$$u = \frac{\tau[n] - \tau[n-k]}{k} \quad (15)$$

Under the hypothesis that u changes slowly, the last seen u can be used to predict τ during the holdover.

B. Kalman filter

In the previous section, the PPS signal was considered as perfect. In reality, this signal from the GPS receiver is subject to jitter, which creates noise in the frequency and offset measurement. According to [26], the RMS of the timing accuracy is 30ns. While this noise can be neglected when the GPS receiver is always on, it is not the case in the holdover mode. Indeed, the absolute offset error is the sum of the offset errors over time. The offset error growth, during holdover, depends on the accuracy of the measured frequency of the local oscillator at the beginning of the holdover.

To filter the noise on the PPS signal when the GPS is on, a Kalman filter was implemented. This filter uses the good short term accuracy of the local clock to filter the noisy PPS observations. The behavior of the fake PPS period τ during the short GPS on-time period is modeled by a random walk process:

$$\tau[n+1] = \tau[n] + v[n] \quad \text{with} \quad v[n] \sim N(0, \sigma_v^2) \quad (16)$$

Let z be the observations of τ from the noisy PPS signal:

$$z[n] = \tau[n] + w[n] \quad \text{with} \quad w[n] \sim N(0, \sigma_w^2) \quad (17)$$

The Kalman filtering process is based on the classical following equations [27]:

- Prediction:

$$\hat{\tau}_{n+1|n} = \hat{\tau}_{n|n} \quad (18)$$

$$p_{n+1|n} = p_{n|n} + q \quad (19)$$

- Update:

$$\tilde{y}_n = z[n] - \hat{\tau}_{n|n-1} \quad (20)$$

$$s_n = p_{n|n-1} + r \quad (21)$$

$$k_n = p_{n|n-1} \cdot s_n^{-1} \quad (22)$$

$$\hat{\tau}_{n|n} = \hat{\tau}_{n|n-1} + k_n \tilde{y}_n \quad (23)$$

$$p_{n|n} = (1 - k_n) \cdot p_{n|n-1} \quad (24)$$

With $q = \sigma_v^2$ and $r = \sigma_w^2$. This filter is stable [28]. The state variable is initialized with the observation. The variables r , q and p_0 are chosen empirically.

V. RESULTS AND DISCUSSION

To evaluate the synchronization algorithms detailed in the previous section, an experimental setup has been developed. Two wireless nodes based on the architecture detailed in section III were implemented on raspberry pi and spartan 6 development boards with their digital inputs connected to the same output of a low-frequency signal generator. This generator generates rising edges (i.e. events) every 2.34 sec that are timestamped by the nodes.

The nodes were placed indoor and the GPS antennas on the roof of the building. The fixed mode was used on the GPS receivers [26]. This GPS configuration is available on certain timing receivers from Ublox. It allows the user to define the GPS antenna location in the receiver to enhance the local time estimation and thus deliver a better PPS signal. The nodes recorded events during more than 2 days. Over 2×10^5 frequency and offset samples were recorded for each node as well as up to 8.5×10^4 event samples.

A. Clock models comparison

First, we compared the clock models. In Fig. 5 the estimated τ with the CSCM and the LSCM are plotted against the observed τ on a part of the dataset and for $k = 1000$ s. The LSCM seems to be closer to the observations than the CSCM. However, Figure 6, which shows the same variables on another part of the dataset, the CSCM seems closer to the observations. The RMSE of the LSCM and the CSCM for the estimation of τ and θ on the full dataset and for k ranging from 10 to 3000, are summarized in Table I. The RMSE for τ and θ were computed on the difference between the predicted τ and θ and the GPS observations.

We can see from this Table that the LSCM outperforms the CSCM for both τ and θ , when $k > 1000$. The PPS noise explained in Subsection IV-B can be seen in the observations in both figures. The fact that the LSCM yields poorer results than the CSCM for $k \leq 1000$ is most probably due to this PPS noise.

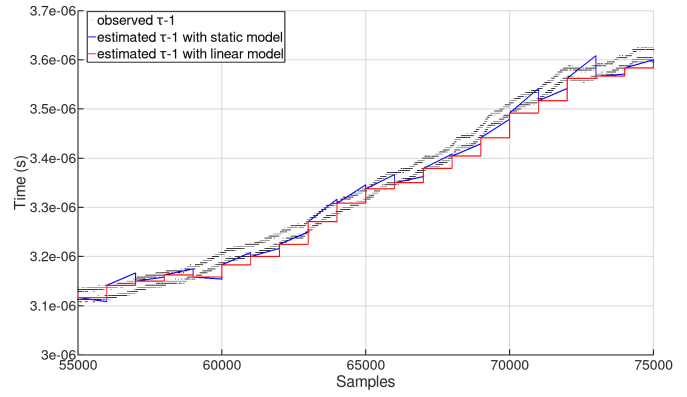


Fig. 5: Observed and predicted τ on the first part of dataset

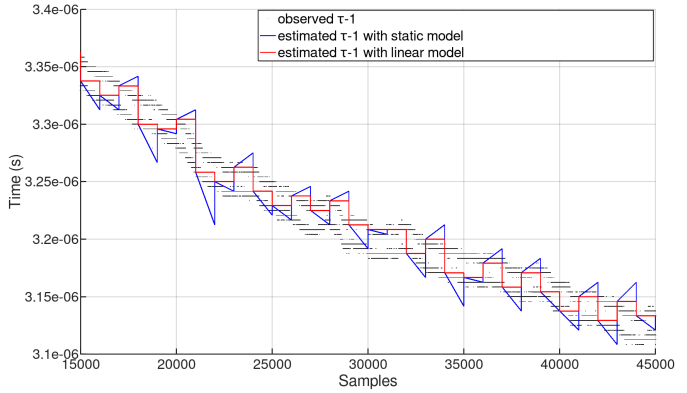


Fig. 6: Observed and predicted τ on the second part of dataset

B. Impact of the Kalman filter

The impact of the Kalman filter on the offset tracking performance was evaluated. As seen in Section IV-B the Kalman filter is only used when the GPS is "on" to filter the PPS noise. Since the performance of the filter depends on the "on" mode duration, the effect of this duration was studied. To do so we ran the Kalman filter for different k_{on} and for different k . Then the on/off ratio r was calculated according to Eq. 5. Figure 7 shows the r against the RMSE of the offset for different values of k_{on} . The RMSE increases as the ratio decrease since a longer holdover yields a poorer synchronization accuracy but a better ratio. From these results

TABLE I: RMSE of the CSCM and LSCM

k	CSCM		LSCM	
	RMSE τ	RMSE θ	RMSE τ	RMSE θ
10	1.3394E-08	5.8209E-08	1.8527E-08	7.8107E-08
25	1.3626E-08	1.4230E-07	1.8483E-08	1.9750E-07
50	1.3656E-08	2.8072E-07	1.8467E-08	3.9577E-07
100	1.3855E-08	5.7021E-07	1.8680E-08	8.0479E-07
250	1.4234E-08	1.4609E-06	1.8604E-08	2.0049E-06
500	1.5341E-08	3.1602E-06	1.8715E-08	4.0681E-06
1000	1.9235E-08	7.9718E-06	2.0007E-08	8.6390E-06
2000	2.9425E-08	2.3955E-05	2.5034E-08	2.0925E-05
3000	3.9110E-08	4.6289E-05	3.2004E-08	3.7230E-05

we chose $k_{on} = 5$ seconds since it seems to be the optimal duration for a RMSE ranging from 10ns to 50 μ s. A lower k_{on} slightly improves the ratio for longer holdover but worsen it for shorter ones.

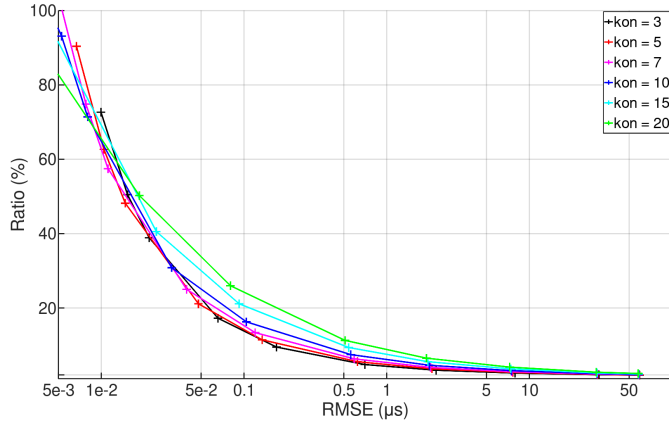


Fig. 7: Optimal k_{on} depending on the ratio r

Figure 8 shows τ for $k = 1000$ s and for the same part of the dataset than in Fig. 6. As can be seen the filtered LSCM seems to fit the observations better than the CSCM. Fig. 9 shows a comparison of the filtered and non-filtered models. The RMSE of the offset is plotted against k . It can be seen that both models can be used for the filtered and non-filtered cases depending on the holdover duration. It can also be seen that the Kalman Filter models yield better results than the non-filtered models. For a holdover duration of less than 134s, the filtered CSCM produces better results, for a holdover duration over 134s the hypothesis of a slowing changing u seems valid and the filtered LSCM yields better results.

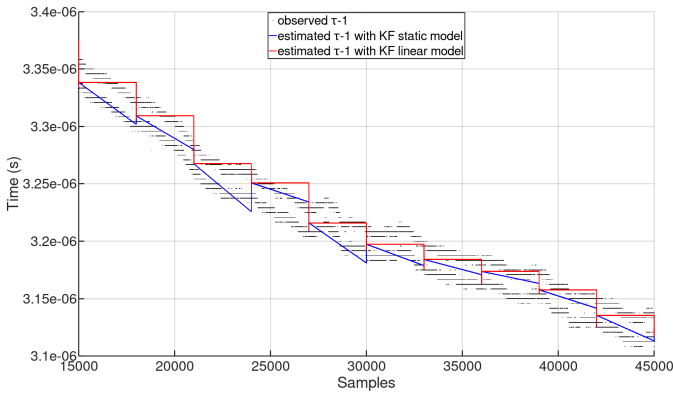


Fig. 8: Observed and predicted τ using a Kalman filter

C. Timestamps

Then we compared the timestamping errors between the different models. The timestamps are computed according to Eq. 2. The timestamp errors are the differences between the timestamps computed with the GPS always "on" and the timestamps computed with the periodic GPS extinctions. Fig. 10 shows the RMSE of the timestamps errors as a function of k for both nodes. As expected the filtered CSCM yields

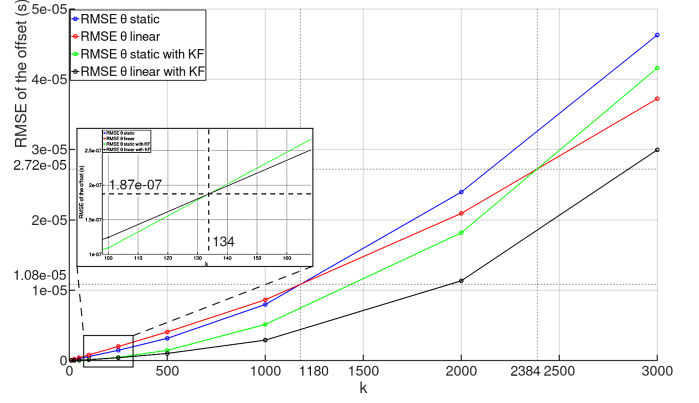


Fig. 9: Offset RMSE for the different models

the best results for holdover up to around $k = 200$ s while the filtered LSCM produces best results above. The evolution of the RMSE as a function of the holdover is approximately the same for both nodes.

Finally, we computed the GPS "on"/"off" ratio for all the models. These ratios are plotted against the RMSE on a semi-log scale, in Fig. 11. It can be seen that for all models the ratio decreases exponentially as the RMSE increases and that they all converge to the limit of 2.5%. This limit corresponds to the minimal GPS ratio according to Eq. 5. The Kalman filter improves the ratio by a factor 3 under the microsecond accuracy despite a longer "on" state. The filtered CSCM yields a maximum improvement of 7% on the ratio over the filtered LSCM under 200s and the gain of the filtered LSCM above is marginal (0.5% max) as it happens for a RMSE greater than 300 ns. The results are similar for both nodes.

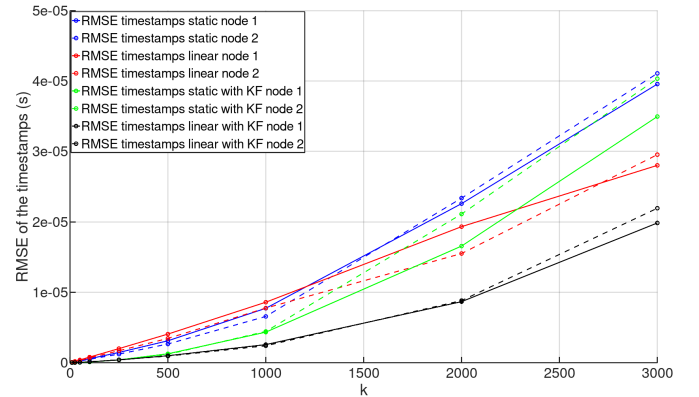


Fig. 10: Timestamps RMSE on both nodes

D. Discussion

Our synchronization solution allows for a RMSE under 10 ns with the GPS always "on". The RMSE stays under 20 ns on both nodes with a GPS "off" 60% of the time. For a GPS "off" 80% of the time and 95% of the time, the RMSEs are under 50 ns and 420 ns, respectively. As the computations were conducted offline (i.e a posteriori) to test different models, the GPS receiver was only virtually off but our study showed that the GPS receiver energy consumption could be divided

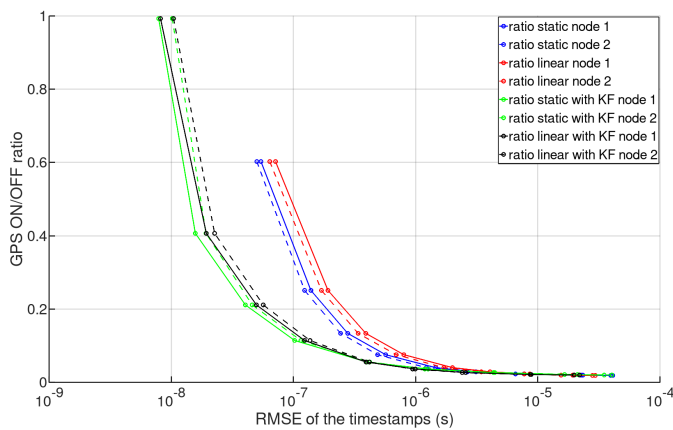


Fig. 11: GPS ratio as a function of timestamps RMSE

by a factor 20 with a mean synchronization error of half a microsecond when implemented with real-time GPS cycling.

However, the data showed that the distribution of the timestamps errors is not exactly normal as it has heavy tails. It was observed that the absolute maximum error is approximately ten times bigger than the RMSE for all our experiments. But even with an accuracy limit ten times bigger than the RMSE, the GPS can be switched off 60% of the time for a maximum error under 200 ns or 95% of the time for a maximum error under 4.2 μ s. Table II summarizes the node to node theoretical range and the accuracy of existing synchronization protocols. TPSN, RBS, or FTSP with Berkley motes can offer μ s synchronization accuracy on small networks with low complexity hardware. Standard IEEE 802.11 synchronization protocols offer the same synchronization accuracy, but sub-nanosecond accuracy can be obtained with the use of PTP. However, the range is still limited to local networks. Sub-nanosecond accuracy can also be obtained with UWB for an even smaller range. For long-range and wide networks, LoRa has been used to obtain 5 μ s accuracy with synchronization updates every 10s. In comparison, the presented GPS based solution has a maximum accuracy of 10 ns (RMSE) and an accuracy of 4.2 μ s for synchronization updates every 100 s.

While dedicated hardware is important for multiple channel high accuracy timestamping, the spartan 6 development board used in this work is not the best target to implement the design as it draws almost as much current as the GPS receiver. But it is only a proof of concept and the timestamp unit can be implemented on a dedicated ASIC or a smaller FPGA or a CPLD. We already implemented this unit on a smaller FPGA (lattice ICE40 [29]) with a slightly lower resolution for a power consumption of 35 mW. For comparison, the ublox receiver needs 150mW when fully ON and the active GPS antenna draws another 10 to 60 mW (depending on the antenna used).

VI. CONCLUDING REMARKS

Synchronization is a challenging problem for wireless nodes, especially for applications requiring good timestamping accuracy across wide areas. Taking into consideration these applications we designed a node with a simple timestamping

Protocol	Theoretical node to node range	Synchronization error	Adaptable accuracy
TPSN [3]	≈ 100 to 300 m (Berkley motes [30])	16.9 μ s avg	no
RBS [2]	≈ 100 to 300 m (Berkley motes [30]) or 20 to 150 m (802.11)	6.29 μ s avg (802.11) 29.1 μ s avg (Mica)	added in [17]
FTSP [4]	≈ 100 to 300 m (Berkley motes [30])	1.48 μ s avg	no
802.11 TSF [31]	≈ 20 to 150 m	4 μ s avg (< 1 μ s std dev)	no
802.11 TA [31]	≈ 20 to 150 m	0.5 μ s avg (2.5 μ s std dev)	no
PTP over 802.11 [5]	≈ 20 to 150 m	240 ps avg (531 ps std dev)	no
Sync. with UWB [6]	≈ 10 m	374 ps avg (677 ps std dev)	no
Sync. with LoRa [23]	≈ 1 to 15 kms	5 μ s max	no
Presented solution	illimited	10 ns RMSE	yes

TABLE II: Range and accuracy of synchronization protocols

dedicated hardware that uses GPS for synchronization. In order to adapt the energy cost of the GPS receiver to the timestamping accuracy needed by the applications, we developed a synchronization scheme based on periodic GPS extinction.

We found that both proposed models can be used depending on the timestamping accuracy needed. For a timestamp RMSE shorter than 300 ns, the constant skew model shows longer holdovers and for a RMSE above the 300ns, the linear model shows longer holdovers. However, it was shown that since most of the GPS ratio gains occur before 300 ns, the linear model yields minor improvements in terms of energy consumption. As expected the use of a Kalman filter to reduce the GPS noise improves the estimation of the local oscillator frequency and thus allows for longer holdover. But we also showed that this holdover length gain compensates for the longer required "on" state duration and overall the filtered models yield better GPS "on"/"off" ratios. We demonstrated that our solution can significantly reduce the energy cost of the GPS receiver depending on the required synchronization accuracy.

In future works, "online" implementations of our solution will be studied to evaluate the gains in energy consumption. Another interesting direction will be the automatic interruption of the holdover according to ambient temperature measurements. This could improve our synchronization scheme, especially for long holdovers, since it was observed that quick temperatures changes can lower the prediction accuracy. Finally, the use of time to digital converters will be investigated as it could allow us to lower the clock frequency inside the FPGA while maintaining, or even improving, the granularity.

REFERENCES

- [1] J. R. Vig, "Introduction to quartz frequency standards," U.S. Army Electronics Technology and Devices Lab., NJ, USA, SLCET-TR-92-1, Tech. Rep., 1992.

- [2] J. Elson, L. Girod, and D. Estrin, "Fine-grained network time synchronization using reference broadcasts," *ACM SIGOPS Operating Systems Review*, vol. 36, pp. 147–163, Dec. 2002, 10.1145/844128.844143.
- [3] S. Ganeriwal, R. Kumar, and M. B. Srivastava, "Timing-sync protocol for sensor networks," in *Proc. SenSys*, Los Angeles, CA, USA, Nov. 2003, pp. 138–149.
- [4] M. Maróti, B. Kusy, G. Simon, and A. Lédeczi, "The flooding time synchronization protocol," in *Proc. SenSys*, New York, NY, USA, Nov. 2004, pp. 39–49.
- [5] R. Exel, "Clock synchronization in ieee 802.11 wireless lans using physical layer timestamps," in *IEEE Int. Symp. on Precision Clock Synchronization*, San Francisco, CA, USA, Sep. 2012, pp. 1–6.
- [6] T. Beluch, D. Dragomirescu, and R. Plana, "A sub-nanosecond synchronized mac-phy cross-layer design for wireless sensor networks," *Elsevier Ad hoc networks*, vol. 11, no. 3, pp. 833–845, Oct. 2012, <https://doi.org/10.1016/j.adhoc.2012.09.010>.
- [7] V. Le Cam, M. Döhler, M. Le Pen, I. Guéguen, and L. Mevel, "Embedded subspace-based modal analysis and uncertainty quantification on wireless sensor platform pegase," in *EWSHM*, Spain, Jul. 2016, pp. 1705–1715.
- [8] L. Lamport, "Time, clocks, and the ordering of events in a distributed system," *Commun. ACM*, vol. 21, no. 7, pp. 558–565, Jul. 1978, 10.1145/359545.359563.
- [9] T. Srikanth and S. Toueg, "Optimal clock synchronization," *J. ACM*, vol. 34, no. 3, pp. 626–645, Jul. 1987, 10.1145/28869.28876.
- [10] D. L. Mills, "Internet time synchronization: the network time protocol," *IEEE Trans. Commun.*, vol. 39, no. 10, pp. 1482–1493, Oct. 1991, 10.1109/26.103043.
- [11] K. B. Lee and J. Eldson, "Standard for a precision clock synchronization protocol for networked measurement and control systems," in *2004 Conf. IEEE 1588, Standard for a Precision Clock Synchronization Protocol for Networked Measurement and Control Systems*, 2004.
- [12] J. Serrano, M. Lipinski, T. Wlostowski, E. Gousiou, E. van der Bij, M. Cattin, and G. Daniluk, "The white rabbit project," 2013.
- [13] J. Van Greunen and J. Rabaey, "Lightweight time synchronization for sensor networks," in *Proc. ACM WSN*, San Diego, CA, USA, Sep. 2003, pp. 11–19.
- [14] K. Römer, "Time synchronization in ad hoc networks," in *MobiHoc*, CA, USA, Oct. 2001, pp. 173–182.
- [15] M. L. Sichitiu and C. Veerarittiphan, "Simple, accurate time synchronization for wireless sensor networks," in *IEEE WCNC*, vol. 2, New Orleans, LA, USA, Mar. 2003, pp. 1266–1273.
- [16] J. M. Rabaey, J. Ammer, T. Karalar, Suetfei Li, B. Otis, M. Sheets, and T. Tuan, "Picoradios for wireless sensor networks: the next challenge in ultra-low power design," in *IEEE Int. Solid-State Circuits Conf.*, San Francisco, CA, USA, Feb. 2002, pp. 200–201.
- [17] S. PalChaudhuri, A. K. Saha, and D. B. Johnson, "Adaptive clock synchronization in sensor networks," in *Proc. IPSN*, Berkeley, CA, USA, Apr. 2004, pp. 340–348.
- [18] D. Djenouri and M. Bagaa, "Synchronization protocols and implementation issues in wireless sensor networks: A review," *IEEE Syst. J.*, vol. 10, no. 2, pp. 617–627, Jun. 2016, 10.1109/JSYST.2014.2360460.
- [19] Y.-C. Wu, Q. Chaudhari, and E. Serpedin, "Clock synchronization of wireless sensor networks," *IEEE Signal Process. Mag.*, vol. 28, no. 1, pp. 124–138, Jan. 2011, 10.1109/MSP.2010.938757.
- [20] D. Cox, E. Jovanov, and A. Milenkovic, "Time synchronization for zigbee networks," in *South. Symp. Sys. Theory*, Tuskegee, AL, USA, Mar. 2005, pp. 135–138.
- [21] A. Mahmood, R. Exel, H. Trsek, and T. Sauter, "Clock synchronization over ieee 802.11—a survey of methodologies and protocols," *IEEE Trans. Ind. Informat.*, vol. 13, no. 2, pp. 907–922, Apr. 2017, 10.1109/TII.2016.2629669.
- [22] A. Mahmood, R. Exel, and T. Sauter, "Performance of ieee 802.11's timing advertisement against synctsf for wireless clock synchronization," *IEEE Trans. Ind. Informat.*, vol. 13, no. 1, pp. 370–379, Feb. 2017, 10.1109/TII.2016.2521619.
- [23] S. Gao, X. Zhang, C. Du, and Q. Ji, "A multichannel low-power wide-area network with high-accuracy synchronization ability for machine vibration monitoring," *IEEE Internet Things J.*, vol. 6, no. 3, pp. 5040–5047, Jun. 2019.
- [24] V. Le Cam, A. Bouche, and D. Pallier, "Wireless sensors synchronization: an accurate and deterministic gps-based algorithm," in *IWSHM*, , USA, Sep. 2017.
- [25] B. R. Hamilton, X. Ma, Q. Zhao, and J. Xu, "Aces: adaptive clock estimation and synchronization using kalman filtering," in *Proc. ACM MobiCom*, San Fransisco, CA, USA, Sep. 2008, pp. 152–162.
- [26] *NEO6T*, ublox. [Online]. Available: [https://www.u-blox.com/sites/default/files/products/documents/LEA-NEO-6T_ProductSummary_\(UBX-13003351\).pdf](https://www.u-blox.com/sites/default/files/products/documents/LEA-NEO-6T_ProductSummary_(UBX-13003351).pdf)
- [27] I. Reid. (2001) Estimation ii. [Online]. Available: <http://www.robots.ox.ac.uk/~ian/Teaching/Estimation/LectureNotes2.pdf>
- [28] C. De Souza, M. Gevers, and G. Goodwin, "Riccati equations in optimal filtering of nonstabilizable systems having singular state transition matrices," *IEEE Trans. Autom. Control*, vol. AC-31, no. 9, pp. 831–838, Sep. 1986, 10.1109/TAC.1986.1104415.
- [29] Lattice ice40 datasheet. [Online]. Available: http://www.latticesemi.com/Products/FPGAandCPLD/iCE40?ActiveTab=Data+Sheet#_21E33C7EC0BD48AA80FE384ED73CC895
- [30] M. Ruiz-Sandoval, T. Nagayama, and B. Spencer Jr, "Sensor development using berkeley mote platform," *J. Earthquake Engineering*, vol. 10, no. 02, pp. 289–309, Mar. 2006, 10.1142/S136324690600261X.
- [31] IEEE, *IEEE Standard for Information Technology-Telecommunications and Information Exchange Between Systems Local and Metropolitan Area Networks-Specific Requirements - Part 11: Wireless LAN Medium Access Control (MAC) and Physical Layer (PHY) Specifications*, IEEE Std. 2012.